Quadrupolar effects on nuclear spins of neutral arsenic donors in silicon

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We present electrically detected electron nuclear double resonance measurements of the nuclear spins of ionized and neutral arsenic donors in strained silicon. In addition to a reduction of the hyperfine coupling, we find significant quadrupole interactions of the nuclear spin of the neutral donors of the order of 10 kHz. By comparing these to the quadrupole shifts due to crystal fields measured for the ionized donors, we identify the effect of the additional electron on the electric field gradient at the nucleus. This extra component is expected to be caused by the coupling to electric field gradients created due to changes in the electron wave function under strain.

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The electron and nuclear spins of donors in silicon have evolved as promising candidates for quantum applications, with extremely long coherence times [1–4], detection down to the single-spin level [5,6], electrical control [7–10], and coupling to superconducting resonators [11,12]. One of the challenges in the design of the involved nanostructures is the generation of uncontrolled mechanical stress due to material interfaces formed by insulators, metal gates, or superconducting resonators with the Si host crystal. These stresses are often distributed over a broad range and can be hard to predict; still their influence has to be considered for a correct quantitative description of the quantum system [13,14].

The influence of strain on the wave functions of donors in silicon has long been known [15]. When stress is applied along the direction of two of the conduction band minima, the energy of these minima is lowered, breaking the sixfold degeneracy of the conduction band and leading to a mixing of the electronic ground state of the donor with excited states. Because of the ensuing changes to the wave function, the hyperfine coupling constant \( A \), which is proportional to the probability density at the nucleus \( |\langle \psi(0) \rangle|^2 \), is reduced, as has been shown experimentally [15,16] and suggested as a possible tuning mechanism for qubits [17]. In electron spin resonance (ESR) experiments at weak magnetic fields [13,18] or on donors with strong hyperfine coupling, such as bismuth in silicon [4,13], a mixing of electron and nuclear spin states leads to a significant influence of the nuclear magnetic resonance (NMR) properties on the ESR measurements [4,19]. For donors with nuclear spin \( I > 1/2 \), therefore, the quadrupole interaction with electric field gradients has to be considered, in particular when strains are involved. While interactions with crystal field gradients cancel out in the cubic symmetry of unstrained silicon, they can significantly shift the NMR of ionized donors under strain and shear [20]. For donors in their neutral charge state, the mixing with excited states under strain breaks the symmetry of the wave function, which could lead to an additional nonzero quadrupolar effect due to field gradients connected to the electron charge distribution [21]. NMR shifts due to these two mechanisms, crystal fields and changes to the electronic wave function, are not easily separated experimentally, as their influence on the observed spectra would be expected to be qualitatively equal. The necessary theoretical treatment, however, is different. While the effect of crystal fields is connected to local changes to bonds with neighboring Si atoms, the symmetry breaking of the wave function can be described by treating the host material as a dielectric continuum [15]. In this work, we measure the NMR of neutral arsenic donors in strained silicon and identify quadrupole shifts of the resonance lines. We compare these to the shifts observed for the NMR of ionized donors in the same samples and find evidence for a component that is observed only in the neutral charge state and should be connected to changes in the wave function.

The Hamiltonian \( \mathcal{H} \) characterizing neutral arsenic donors with electron spin \( S = \{S_x, S_y, S_z\} \) and nuclear spin \( I = \{I_x, I_y, I_z\} \) consists of four different interactions, here ordered by their typical strengths from highest to lowest energy:

\[
\mathcal{H}/\hbar = f_0 S_z + A S \cdot I - \nu_0 I_z + v_Q \frac{1}{2} \left( I_z^2 - \frac{5}{4} \right),
\]

where \( h \) is Planck's constant. The terms describe (i) the Zeeman interaction of the electron spin with an external magnetic field \( B_z \), with the electronic gyromagnetic ratio \( \gamma_e \); (ii) the hyperfine interaction of the electron and nuclear spins, where \( A = 198.35 \text{ MHz for As in Si} \) [22]; (iii) the nuclear Zeeman interaction, where \( \nu_0 = \gamma_n B_z \), with the nuclear gyromagnetic ratio \( \gamma_n \); and (iv) the nuclear quadrupole interaction with an effective electric field gradient \( V_{33} \), here approximated to first order, with

\[
h\nu_Q = \frac{1}{2} V_{33} e Q \times \frac{1}{2} (3 \cos^2 \vartheta - 1).
\]

where \( Q \) is the nuclear quadrupole moment and \( e \) is the elementary charge [23]. The second term on the right-hand side of (2) describes the dependence on the angle \( \vartheta \) between \( B_z \) and \( V_{33} \) and varies between 1 for \( \vartheta = 0^\circ \) and \( -1/2 \) for \( \vartheta = 90^\circ \).

In a nonzero magnetic field, the eigenstates of \( \mathcal{H} \) split up into two subensembles with electron spin projections \( m_S = 1/2 \) and \( -1/2 \), which are further divided into four levels with different nuclear spin projections \( m_I = 3/2 \cdots -3/2 \) [cf. Fig. 1(a), not to scale]. The transitions which are allowed by NMR selection rules (\( \Delta m_S = 0, \Delta m_I = \pm 1 \)) are labeled 1 through 6. In the limit of high magnetic fields
and without quadrupole interactions the transition frequencies $\nu_{mS} = |mS A - \nu_0|$ are equal within each subensemble. While the high-field limit is not reached in the experiments below, it still allows us to discuss the qualitative changes expected due to changes in the different coupling constants. For a reduction of the hyperfine constant $A$, we expect similar shifts towards lower frequencies for all six transitions. On the other hand, a change in $\nu_0$ should act on the two subensembles with different signs. The influence of the first-order quadrupole interaction is sketched in the last column (“quadrupole interaction”) of Fig. 1(a). While there is no effect on the two central transitions 2 and 5, the satellite transitions are shifted by $+\nu_Q$ (1 and 6) and $-\nu_Q$ (3 and 4). Quantitatively this is shown in Fig. 1(b), where the six transition frequencies for arsenic donors are plotted as a function of the magnetic field with (dashed lines) and without (solid lines) a hypothetical quadrupole interaction of $\nu_Q = 0.5$ MHz.

The samples used in this work are Czochralski-grown silicon wafers implanted with As$^+$ ions at low energies. This creates a doped region with a depth of $\sim 50$ nm below the surface. As part of the implantation damage, oxygen-vacancy complexes are formed, which, in their excited triplet state (SL1), are an efficient recombination partner for As donors [24,25]. This allows us to perform electrically detected magnetic resonance experiments providing the high sensitivity needed. The samples (size $\sim 10 \times 3 \times 0.5$ mm$^3$) remained unannealed, were contacted with Cr/Au interdigit structures, and biased with typically 5 V. Electrically detected electron nuclear double resonance (ENDOR) measurements were performed in a Bruker flexline resonator for pulsed ENDOR at a temperature of 8 K in a He flow cryostat; illumination was provided by a red light-emitting diode. The detection is performed on the same electron spin resonance line as the selective ionization, which means that we expect a positive signal for neutral nuclear spin resonances and a negative signal for resonances of ionized donors [27].

Figure 2 shows electrically detected ENDOR spectra recorded on the four hyperfine-split electron resonance lines. As expected, the nuclear magnetic resonances of the neutral As donors are observed as an enhancement in signal amplitude. Each measurement is sensitive to transitions which involve the ionization, both ensembles are highly polarized and their NMR transitions can be accessed in the ENDOR experiments. The detection is performed on the same electron spin resonance line as the selective ionization, which means that we expect a positive signal for neutral nuclear spin resonances and a negative signal for resonances of ionized donors [27].

To study the effect of strain on these resonances, samples with different crystal orientations were thinned to $\sim 100 \mu$m and cemented onto 500-\mu m-thick sapphire substrates, which at low temperatures induces strain due to the different thermal expansion coefficients [28,29]. We assume the resulting strain to be uniaxial and normal to the Si/sapphire interface. Note that the angle $\varphi$ between this normal and the magnetic field $B_z$ is not per se equal to $\theta$, which describes the orientation of the generated electric field gradient. Figure 3(a) shows spectra obtained for Si/sapphire stacks with samples from [100] and [111] wafers. Compared to the line position of an unstrained sample, both As$^+$ related resonances in each of the spectra are shifted towards lower frequencies. This indicates that the dominant effect on the line position is a reduction of the hyperfine coupling to the donor electron and not a quadrupole interaction, which would shift the two lines of each spectrum in different directions (cf. Fig. 1). Such a reduction of the hyperfine constant $A$ is expected for strain that lifts the symmetry of the six conduction band minima in silicon, which is expected for our [100] sample. More quantitatively, $A(\chi)/A(0) = \frac{1}{2}[(\frac{\chi}{3} + 1)/2 + (\frac{\chi}{3} + \frac{\chi}{3} + 1)^{1/2} + 1]$ with the unitless valley strain $\chi$ (cf. Ref. [15]), which is
a measure for the strain-induced asymmetric change of the electron wave function. This leads to asymmetric electric field gradients, which interact with the nuclear spin of the donor via quadrupole interaction. We therefore expect that any quadrupole shift due to the electron wave function is connected to $\chi$. For strain in [111] direction, the energy of all conduction band minima is lowered by the same amount and $\chi = 0$ [15]. Still, we also observe a reduced hyperfine coupling in the [111] sample, suggesting that the strain in the Si/sapphire stack is not purely along the [111] axis and $\chi \neq 0$ also in this case.

At lower frequencies [Fig. 3(b)], the spin resonance of the ionized donors As$^+$ is observed as a negative signal. Since $A = 0$ in this case, the observed As$^+$ NMR frequency $\nu_+ \equiv \nu - \nu_Q^0$ with the quadrupole interaction frequency $\nu_Q^0$ of the ionized donor. For the strained samples, shifts of $\nu_Q^0 = 34(5)$ and $-63(5)$ kHz are observed for the [100] and [111] samples, respectively, in agreement with previous measurements [20] and the expected angular dependence for $\theta = 90^\circ$.

To give a more detailed analysis of the observed resonances of the neutral donors, the peak positions are extracted by fitting with pseudo-Voigt functions (shape factors $\sim 0.5$). For the resulting data, least-square fits to the expected peak positions are performed, using the hyperfine constant $A$ and the nuclear gyromagnetic ratio $\gamma_n$ as fitting parameters. We then plot the deviation of the observed peak position from these fits to study any behavior that cannot well be described considering only these two interactions. The resulting residuals for the As$^0$ NMR in the sample strained along the [100] axis are shown as full circles in Fig. 4(a) for $\varphi = 0^\circ$. Clearly, a systematic deviation from 0 is observed, which is positive and about equal for resonances 1 and 6, negative but of similar absolute value for 3 and 4, and close to zero for resonances 2 and 5. This mirrors the expected shift due to a quadrupole interaction (cf. Fig. 1). When including the term describing the quadrupole interaction in the fit, a significantly better result is obtained (empty circles) and the remaining deviations seem unsystematic and are expected to reflect the experimental noise. The resulting quadrupole shift $\nu_Q^0$ is shown as a blue dashed line in Fig. 4. When the sample is rotated in the magnetic field by $\Delta\varphi = 90^\circ$, the sign of $\nu_Q^0$ changes (data not shown). Performing the same analysis for the data obtained on the [111] Si:As sample for $\varphi = 0^\circ$ (data not shown) and $\varphi = 90^\circ$ [Fig. 4(b)], a similar systematic deviation is observed. Again, the residuals are very well explained by a quadrupolar effect and the measurements at different angles are very well described by the expected angular dependence (2) for an effective electric field gradient generated along the strain axis ($\theta = \varphi$). The constants determined by these fits are summarized in Table I.

To investigate the origin of these quadrupole shifts, we compare them to the shifts $\nu_Q^0$ observed on the ionized donors Si:As$^+$ for each of the samples, which are shown as green dotted lines in Figs. 4(a) and 4(b). For both samples, these shifts are slightly smaller than those observed for the neutral donors $\nu_Q^0$ (blue lines). This suggests that we observe an additional quadrupole interaction connected to the donor electron, the strength of which can be estimated by taking the differences $\Delta \nu_Q = \nu_Q^0 - \nu_Q^0$ of the frequency shifts. The values for both samples are given in Table I. For the [100] sample, $\Delta \nu_Q$ of 31(11) and $-14(18)$ kHz are observed at $\varphi = 0^\circ$ and $90^\circ$, respectively. The factor $\sim -1/2$ between the two measurements is once more in agreement with the expected angular dependence (2), if the electric field gradient $V_{\Delta 33}$ connected to the electron wave function is generated parallel to the strain axis in the [100] direction of our sample. Since the conduction band minima in Si are along the (100) axes, this would indeed be expected. Using (2), we can calculate an electric field gradient $V_{\Delta 33} = 7.8 \pm 10 \times 10^{18}$ V/m$^2$, which is generated upon the application of a uniaxial strain $\varepsilon_1 = 2.3(5) \times 10^{-4}$ along the [100] axis, as calculated from the observed change of the hyperfine coupling [16]. For the [111] sample, $\Delta \nu_Q$ of 21(9) and $-12(9)$ kHz are observed at $\varphi = 0^\circ$ and $90^\circ$, respectively. As discussed above, while in principle no change to the symmetry of the wave function is expected for strain in [111] direction, the reduction of $A$ indicates the presence of a (weaker) valley strain $\chi$, probably due to a slightly different strain axis in our samples. Consequently, a weaker but nonzero $\Delta \nu_Q$ would be expected in this sample as well, which is in agreement with our measurements. The observed shifts correspond to an effective electric field gradient...
at the nucleus $V^\Delta_{33} = 6.1 \pm 5 \times 10^{18} \text{ V/m}^2$ which is generated approximately along the strain axis. Comparing the values for $\chi$ and $V^\Delta_{33}$ measured in the two samples, the observed monotonous and possibly linear dependence strongly suggests that strain components altering the wave-function symmetry are responsible for the observed additional quadrupolar effects in the neutral charge state.

In summary, we report shifts to the NMR of neutral donors in strained silicon which agree with the behavior expected for quadrupolar effects. These shifts differ from the quadrupole shifts due to crystal field gradients which we determine via the NMR of ionized donors and indicate the presence of additional quadrupolar effects.

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