

Silicon isotope engineering for the development of better classical and quantum computers

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Contents

- 1. Silicon semiconductor engineering**
- 2. Better Si chips for classical computers**
 - Highly thermal conductive silicon
 - Probing thermal oxidation mechanism
 - Probing Si diffusion during heat processing
- 3. Superconductivity in $\text{Ba}_8\text{Si}_{46}$ clathrate**
- 4. All silicon quantum computers**
 - ^{29}Si nuclear spins embedded in spin-free ^{28}Si matrix

Collaborators

Isotope engineering:	Eugene E. Haller (UC Berkeley) Hans- J. Pohl (U. Jena)
Oxidation studies:	Tomonori Takahashi (Keio University) Shigeo Fukatsu (Keio University) Masashi Uematsu (NTT Basic Research Lab) Hiroyuki Kageshima (NTT Basic Research Lab) Yasuo Takahashi (NTT Basic Research Lab) Kenji Shiraishi (University of Tsukuba)
Ba ₈ Si ₄₆ clathrate	Tomoko Shimizu (Keio University) Katsumi Tanigaki (Osaka City University)
Si quantum computers	Eisuke Abe (Keio University) Ryusuke Nebashi (Keio University) Yoshinori Matsumoto (Keio University) Hideo Ohno (Tohoku University) Yuzo Ohno (Tohoku University) Susumu Sasaki (Nigata University) Yoshisa Yamamoto (Stanford University) Thaddeus Ladd (Stanford University) Jonathan Goldman (Stanford University) Fumiko Yamaguchi (Stanford University) Anne Verhulst (Stanford University)

1. Semiconductor Isotope Engineering

List of stable isotopes

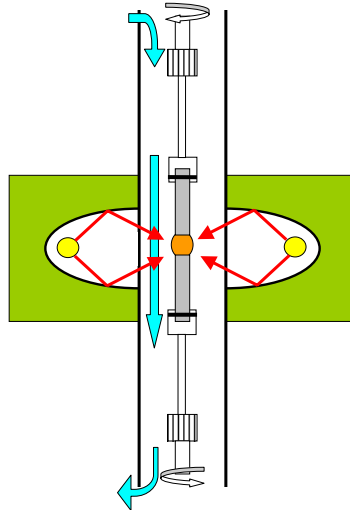
²⁸ Si	92.2%		⁶⁹ Ga	60.1%	→ 3/2
²⁹ Si	4.7%	→ 1/2	⁷¹ Ga	39.9%	→ 3/2
³⁰ Si	3.1%	(nuclear spin)	⁷⁵ As	100%	→ 3/2
⁷⁰ Ge	20.5%				
⁷² Ge	27.4%				
⁷³ Ge	7.8%	→ 9/2			
⁷⁴ Ge	36.5%	(nuclear spin)			
⁷⁶ Ge	7.8%				

Mass and nuclear spin
Control through manipulation
of stable isotopes

Si bulk crystal growth



Floating-zone Si grower



Isotopically controlled Si fabrication

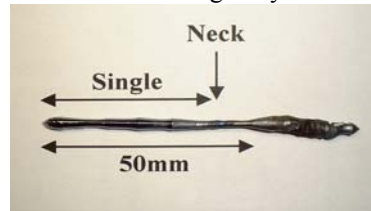
Natural abundance

^{28}Si 92.2%

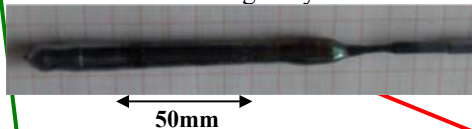
^{29}Si 4.7%

^{30}Si 3.1%

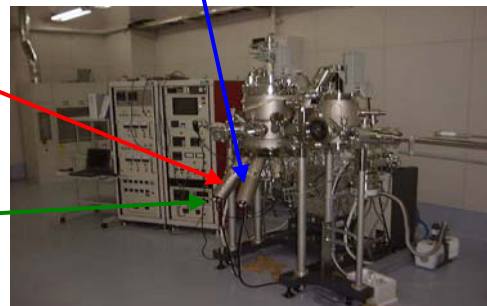
99.92% ^{28}Si single crystal



98.6% ^{29}Si single crystal



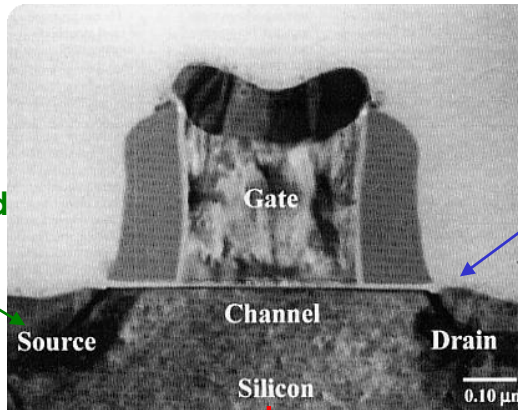
96% ^{30}Si single crystal



2. Better Si chips for classical computers

MOSFET

3. Impurity and Si diffusion

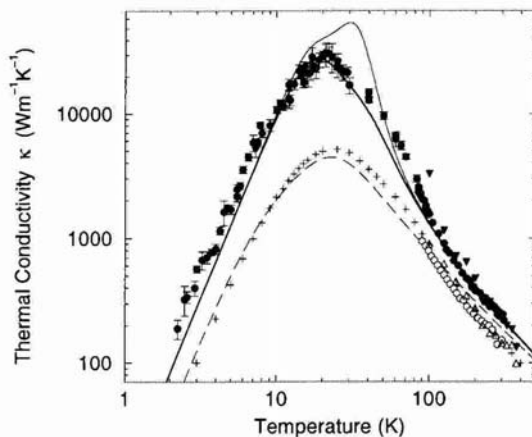


2. SiO₂ formation

1. Heat flow

Isotope effect on thermal conductivity of Si

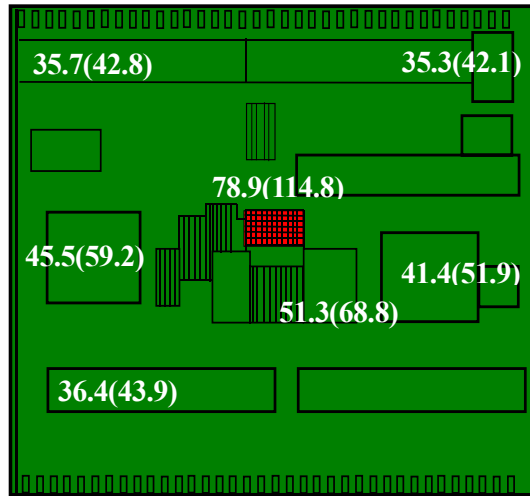
Thermal conductivity of 99.86% ²⁸Si



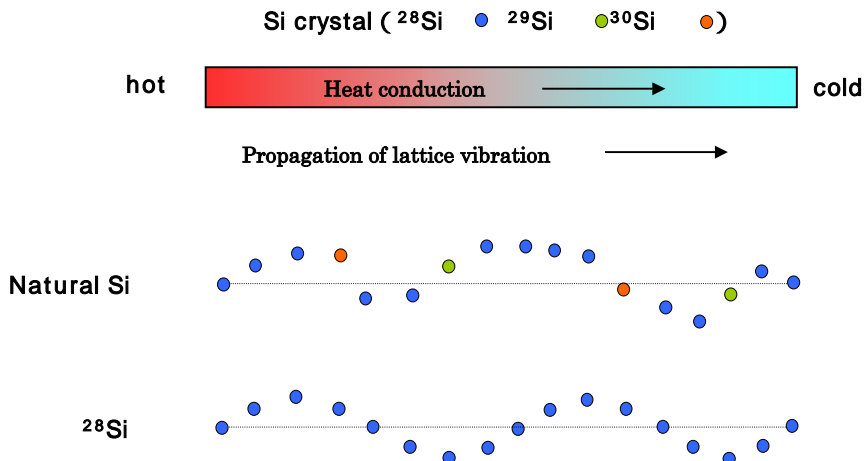
300K 60% increase
400K 40-50% increase
with respect to natural Si

Temperatures in a 1GHz microprocessor (simulation)

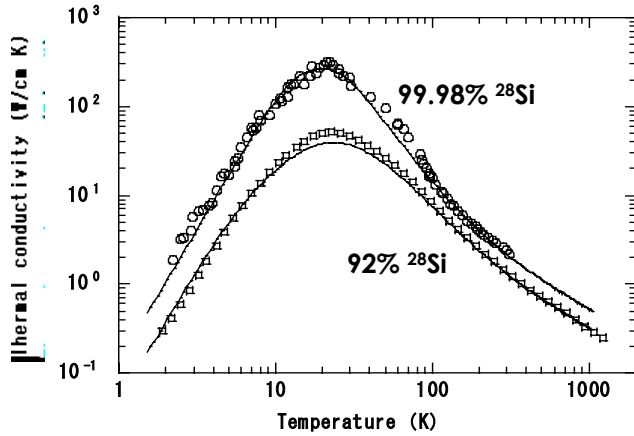
Temperatures in Celsius
for
an isotopically enriched
 ^{28}Si substrates and
a natural Si substrate
in parentheses



Thermal conductivity enhancement



Comparison with theory



1. Isotope scattering

$$g = \frac{\sum c_i M_i^2 - (\sum c_i M_i)^2}{(\sum c_i M_i)^2}$$

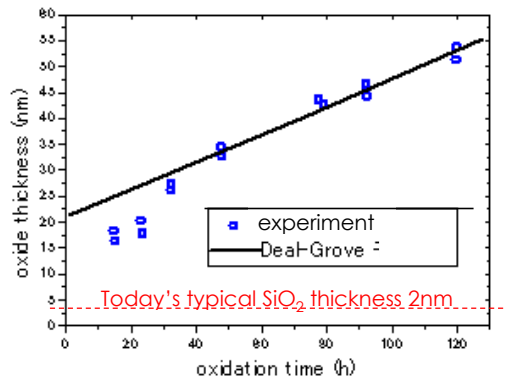
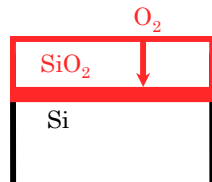
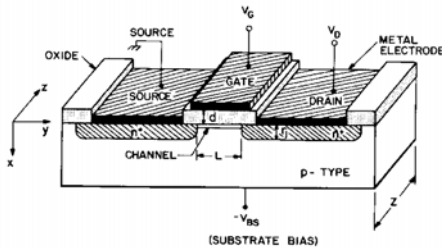
2. Boundary scattering

3. Normal process (phonon)

4. Umklapp process (phonon)

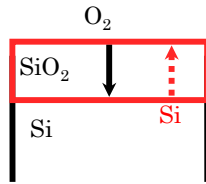
Fit based on M. G. Holland: Phys. Rev. **132** (1963) 2461

Thermal oxidation of Si



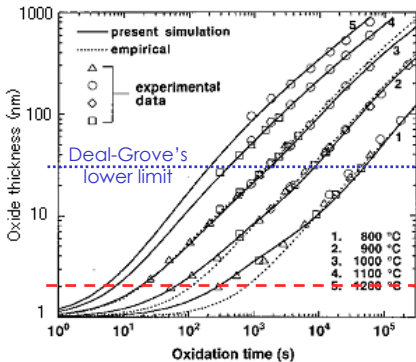
Deal and Grove's model
J.Appl.Phys., **36**.3770(1965)

Does Si diffuse into SiO₂ ?



1. Need to know Si diffusion coefficient in thermally grown SiO₂

2. Need to find Si diffusing into SiO₂ during thermal oxidation

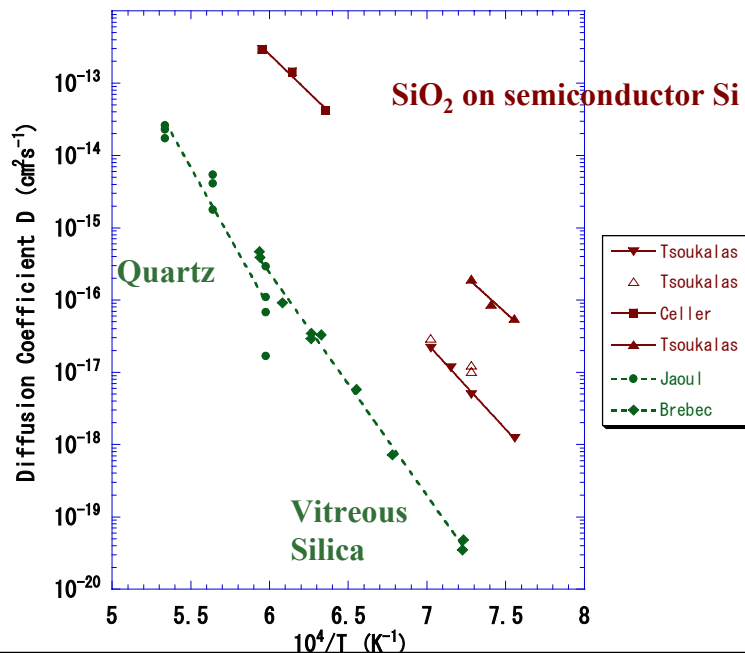


Today's typical SiO₂ thickness 2nm

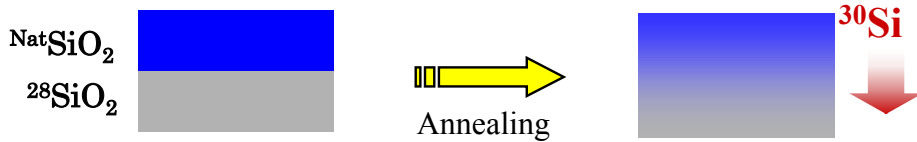
Typical SiO₂ thickness 2nm

M. Uematsu et al. Jpn. J. Appl. Phys. **39** (2000) L699

Self-Diffusion of Si in SiO₂



Diffusion studies with stable isotopes



Isotope Heterostructures

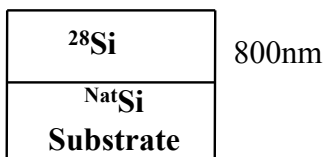
Diffusion of ^{30}Si \Rightarrow SIMS Measurement

Isotope Composition of $^{\text{Nat}}\text{SiO}_2$ and $^{28}\text{SiO}_2$

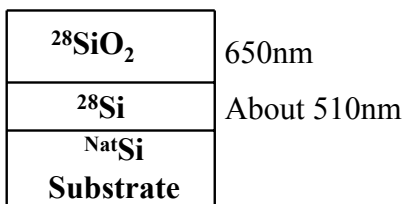
Isotope	^{28}Si	^{29}Si	^{30}Si
$^{\text{Nat}}\text{SiO}_2$	92.2%	4.7%	3.1%
$^{28}\text{SiO}_2$	99.924%	0.073%	0.003%

Preparation of Samples

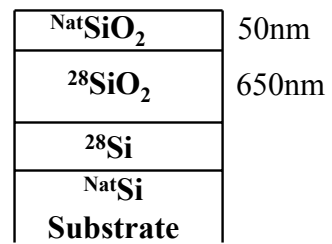
Using $^{28}\text{SiH}_4$



Dry Oxidation



LPCVD
of TEOS



Annealing

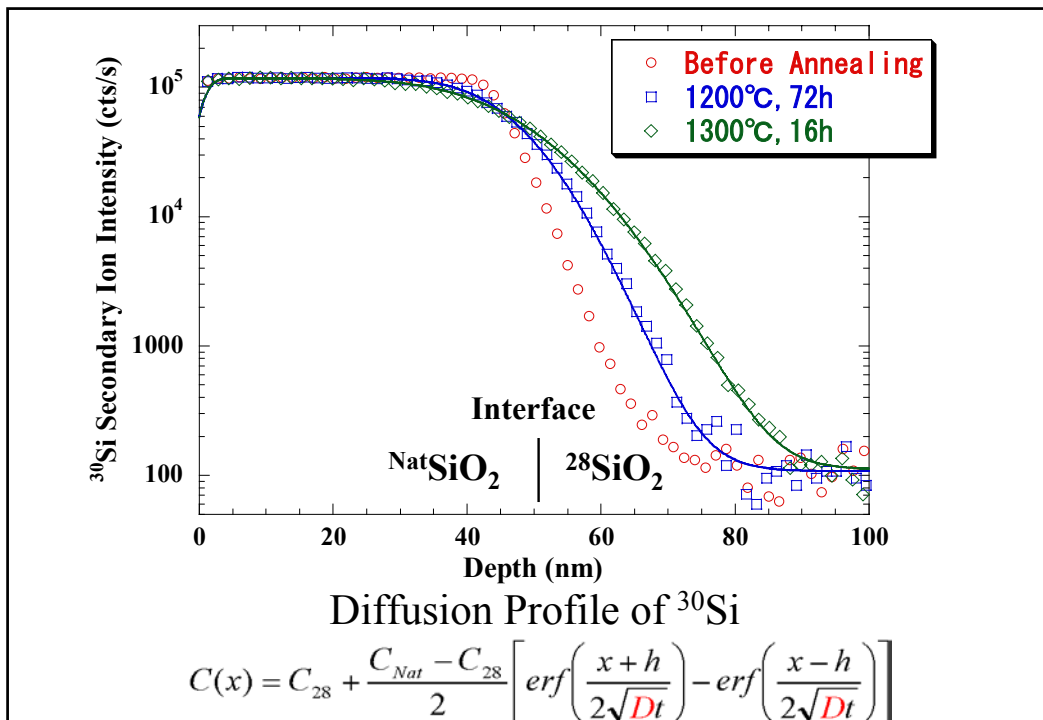
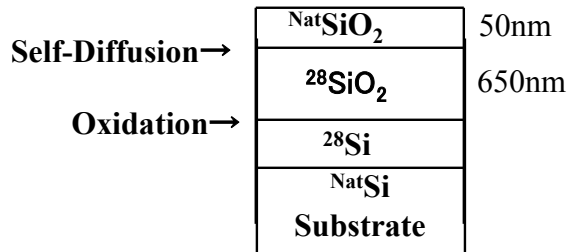
- 1150, 1200, 1250, 1300°C

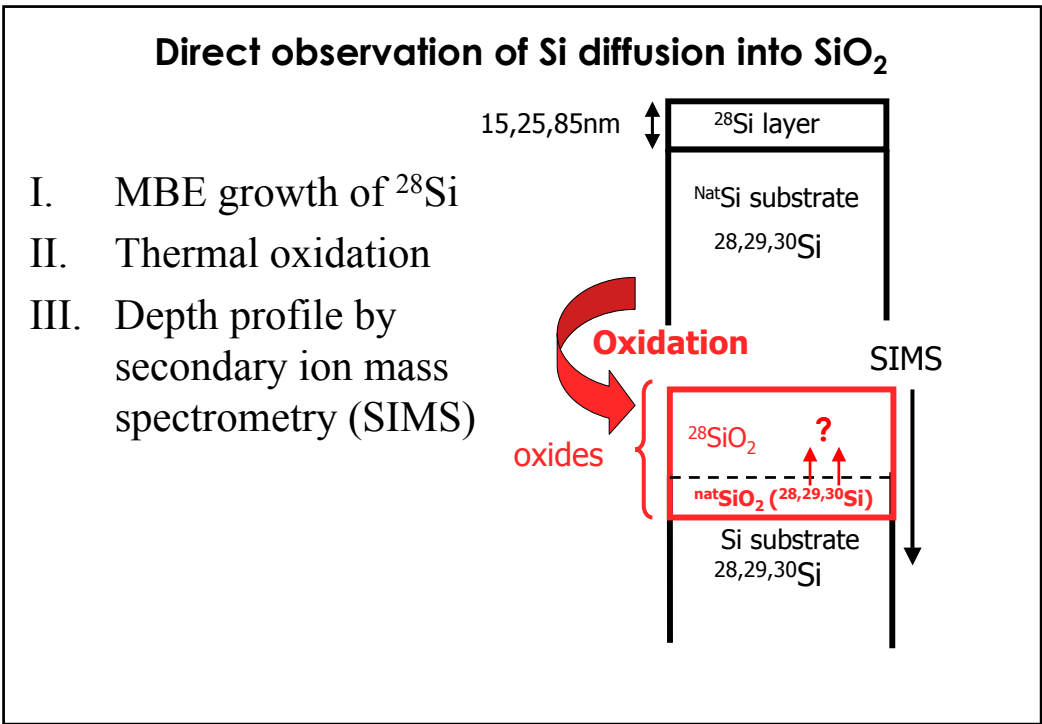
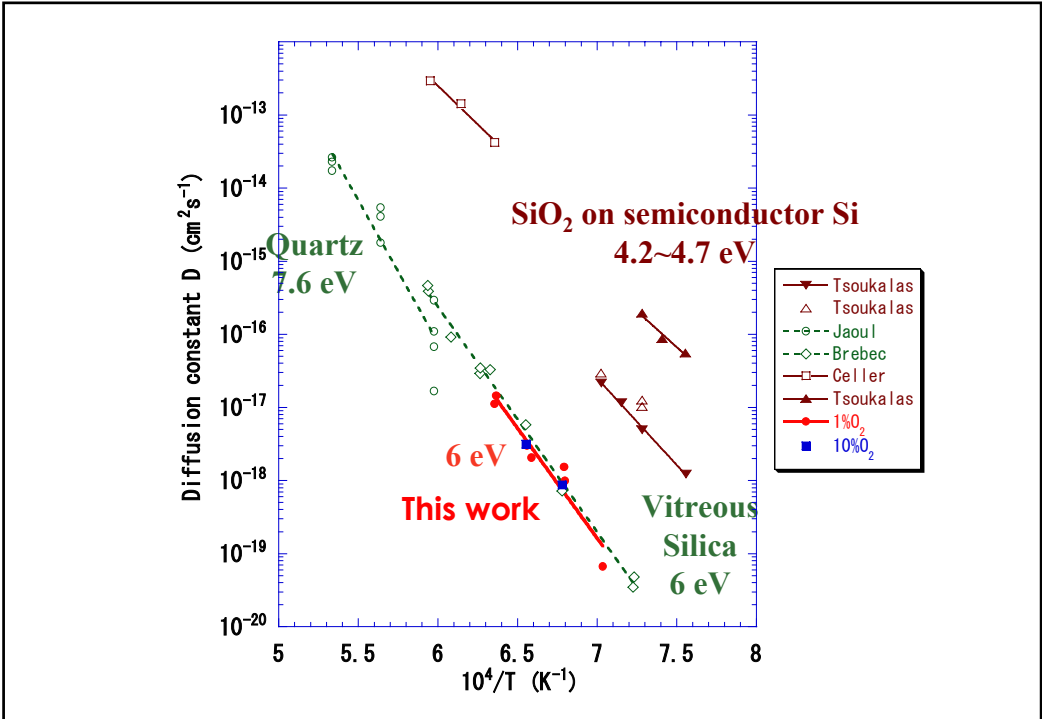
- Flowing Ar+1%O₂

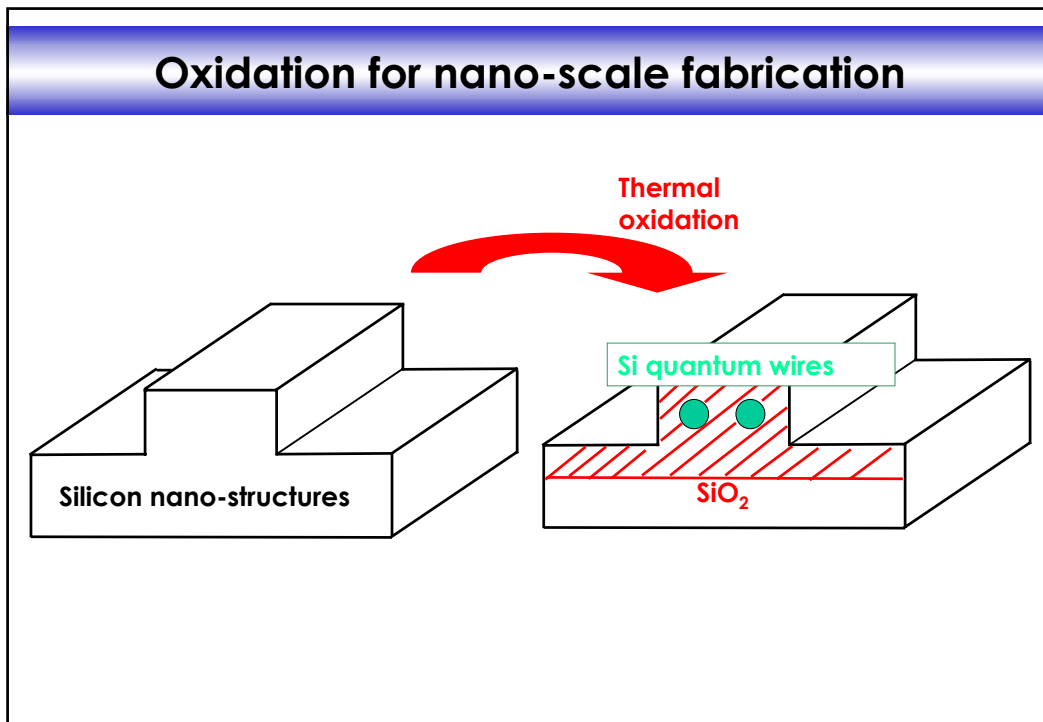
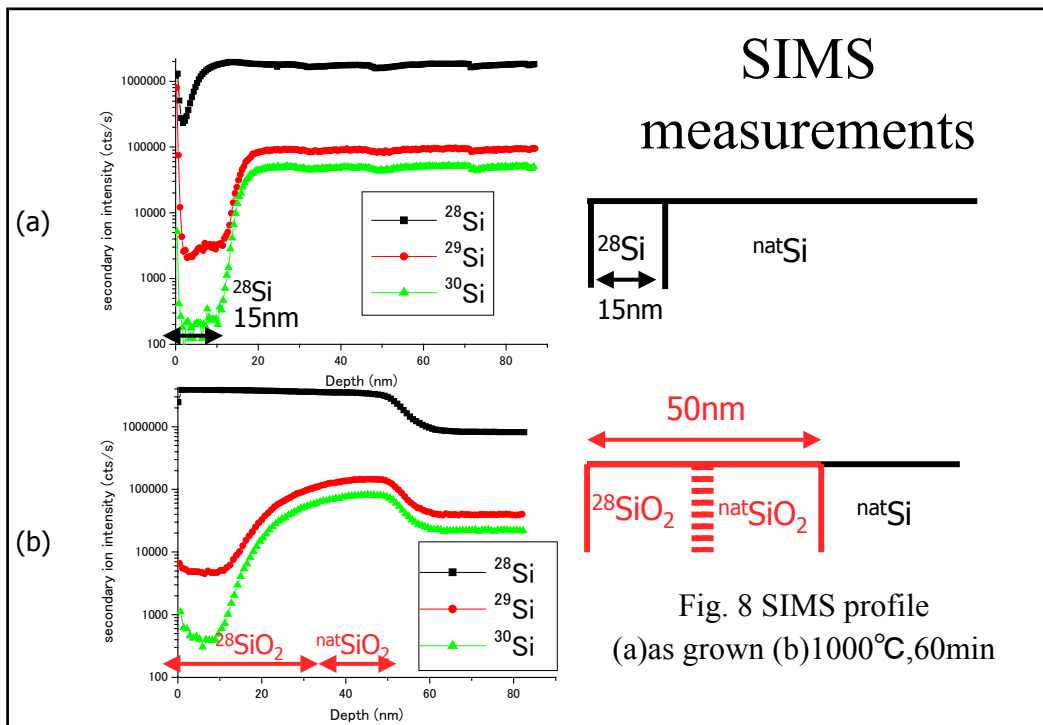
Oxygen prevents decomposition of SiO₂

Concentration of oxygen Low High
 ↓ ↓
 Decomposition Oxidation

- Flowing Ar+20% O₂

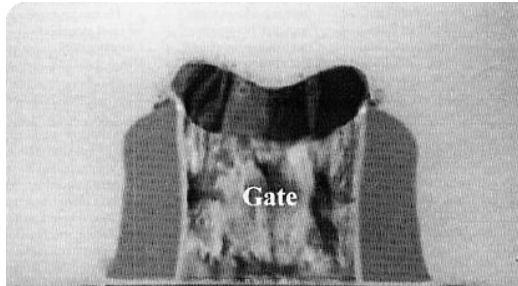






Impurity and Si diffusion

MOSFET



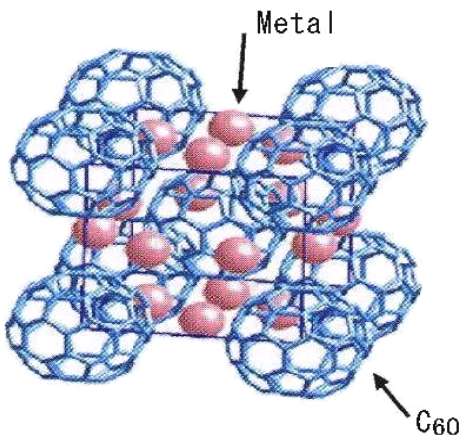
Impurity and Si diffusion

²⁸Si layer

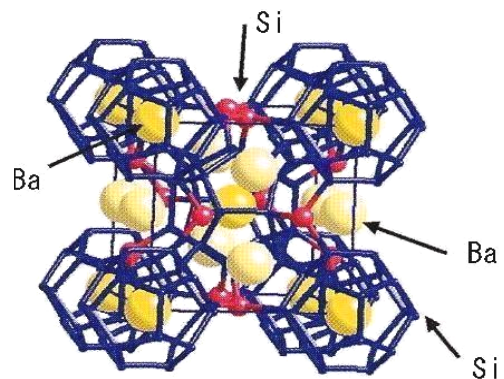


³⁰Si layer

3. Superconductivity in Ba₈Si₄₆ clathrate



(a) M_xC₆₀



(b) Ba₈Si₄₆

Structure of Group IV Clusters

Superconductor Ba₈Si₄₆

Ba doped Si₄₆ Clathrate



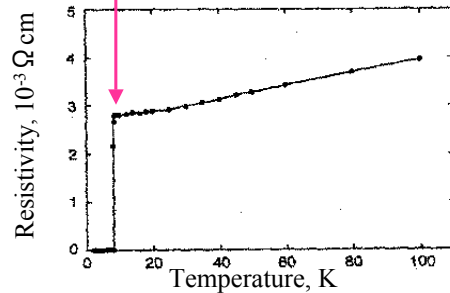
High Pressure Synthesis

Lattice const. ↑ by Ba doping

Strong hybridization between Si₄₆ band and Ba orbital

→ N(E_F) becomes large

Critical Temperature
T_c = 8K



Temperature dependence of the resistivity of Ba₈Si₄₆

S. Yamanaka et al. "High-Pressure Synthesis of a New Silicon Clathrate Superconductor, Ba₈Si₄₆"
Inorg. Chem. 39 (2000) 56

BCS model

$$T_c = 1.14 \frac{\hbar\omega}{k_B} \exp\left(-\frac{1}{N(E_F)V}\right) \propto \omega$$

$$\omega = \sqrt{\frac{k}{m}}$$

Density of states
at the Fermi Level
High (55 states/eV)

e⁻-phonon
Interaction
?

Phonon
frequency

→ check for the isotope effect (²⁸Si and ³⁰Si)

Isotope effect on T_C

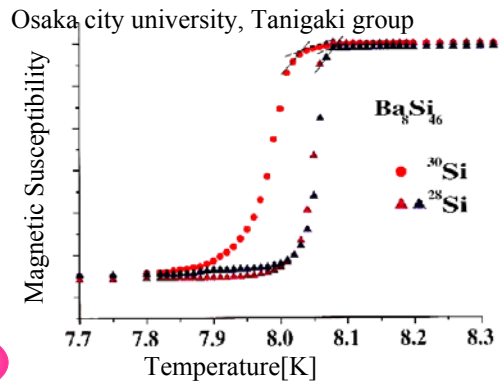
From BCS Theory

$$\begin{aligned} T_C(^{30}\text{Si}) / T_C(^{28}\text{Si}) \\ &= \sqrt{28} / \sqrt{30} \\ &= 0.97 \end{aligned}$$

From Experimental Result

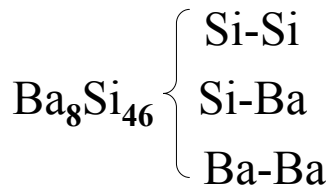
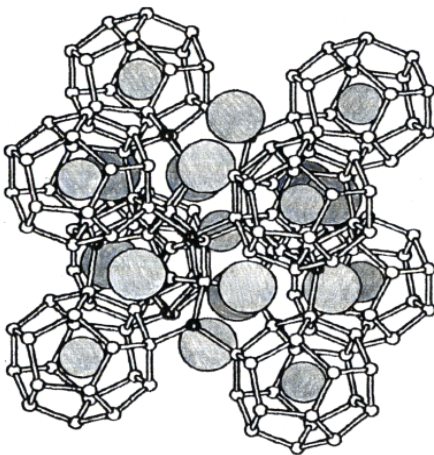
$$\begin{aligned} T_C(\text{Ba}_8^{30}\text{Si}_{46}) / T_C(\text{Ba}_8^{28}\text{Si}_{46}) \\ &= 8.02\text{K} / 8.07\text{K} \\ &= 0.99 \end{aligned}$$

BCS-like

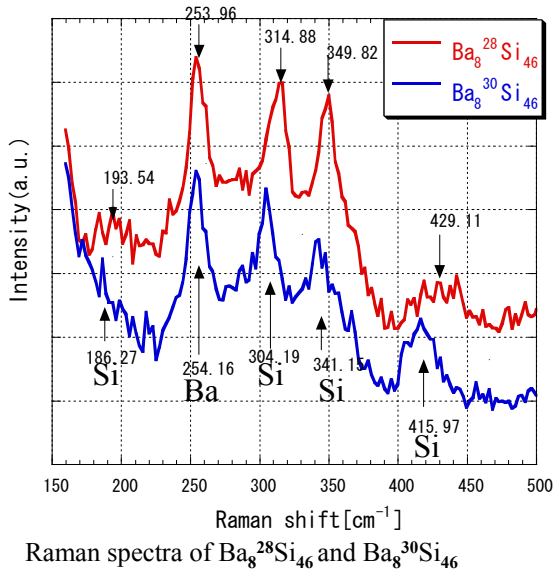


Temperature dependence of Magnetic Susceptibility of $\text{Ba}_8^{28}\text{Si}_{46}$ and $\text{Ba}_8^{30}\text{Si}_{46}$

Raman studies of vibrational modes



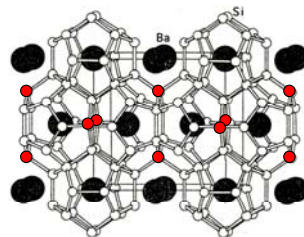
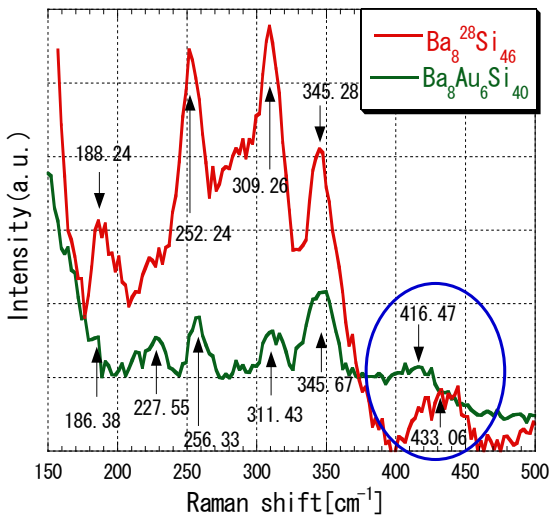
Raman results



5 peaks observed

- 4 shifted
 - ↔ related modes
 - wavenumber ratio
 - $k(30)/k(28)$
 - $= 0.96 \sim 0.98$
 - mass ratio
 - $\sqrt{28}/\sqrt{30} = 0.97$
- 1 does not shift
 - ← Ba related

Raman results



- : c-site Si or Au
- Fermi surface related site
- 430 cm^{-1} peak is related to Si at c-sites



Quantum computation with spins

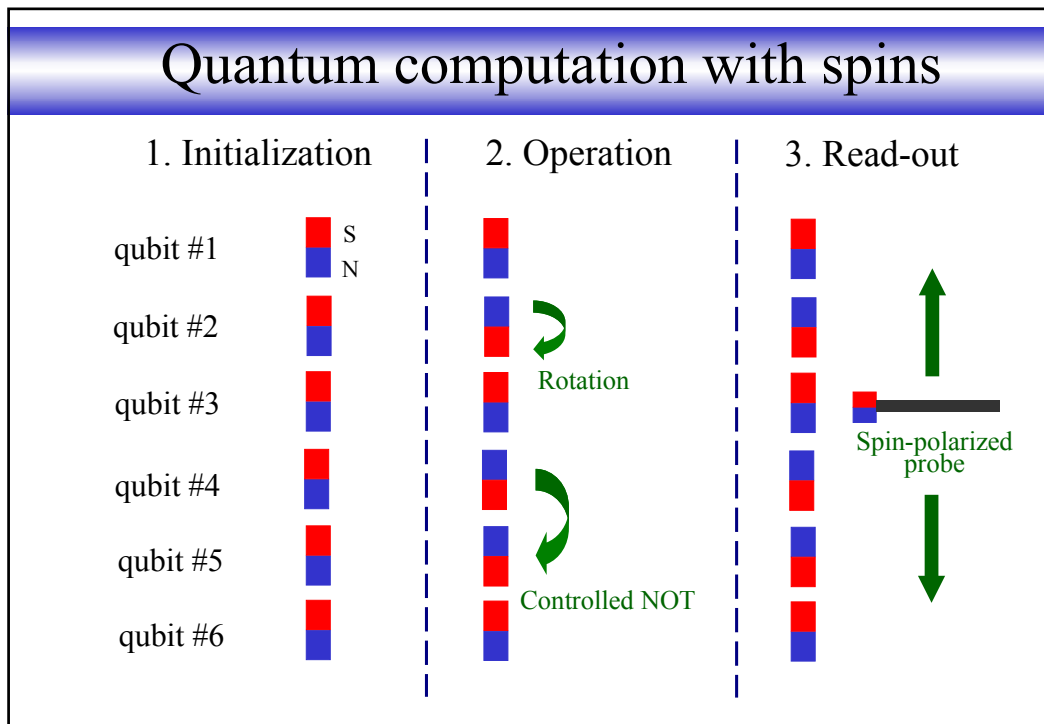


Figure of merits for QC

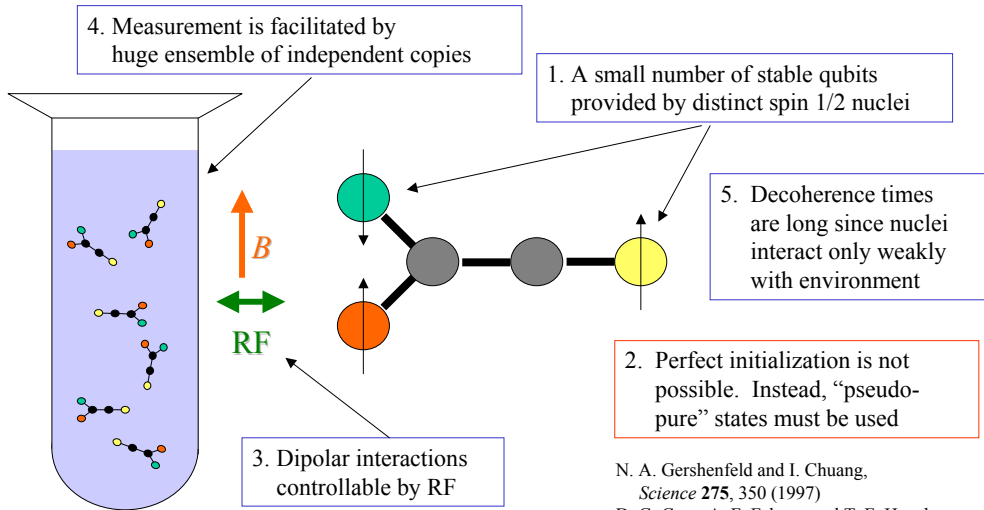
1. Number of qubits: n

available number of states 2^n

2. Maximum total computable steps: N_{\max}

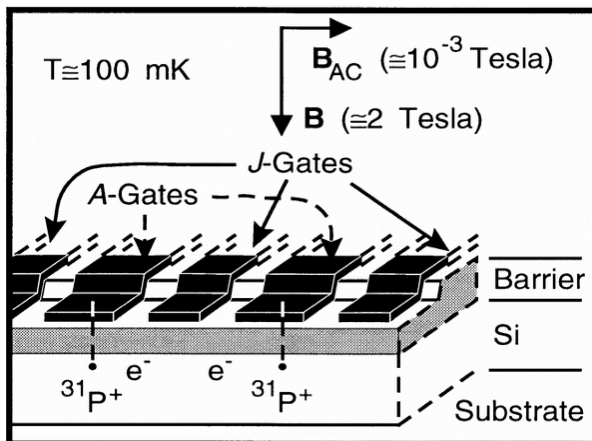
$$N_{\max} = \frac{\text{phase decoherence time: } T_2}{\text{time needed for each operation: } t_s}$$

Solution NMR Quantum Computation



N. A. Gershenfeld and I. Chuang,
Science **275**, 350 (1997)
D. G. Cory, A. F. Fahmy, and T. F. Havel,
Proc. Natl. Acad. Sci. USA **94**, 1634 (1997)

Solid-State Impurity NMR QC



1. Isolated impurity nuclei provide qubits
2. Low temperature electrons allow initialization
3. Electron-mediated interactions controlled by gates
4. Single-spin measurement via nuclear-electron coupling is proposed
5. Well-separated impurities have long decoherence times

B. E. Kane, *Nature* **393**, 133 (1998)

Motivation

Solution NMR QC

N. A. Gershenfeld and I. Chuang,
Science **275**, 350 (1997)
D. G. Cory, A. F. Fahmy, and T. F. Havel,
Proc. Natl. Acad. Sci. USA **94**, 1634 (1997)

Advantages:

Ensemble measurement
Natural (chemical) fabrication

Disadvantages:

Challenging to scale to many
qubits and/or gates
Initialization difficult

Solid-State Impurity QC

B. E. Kane, *Nature* **393**, 133 (1998)
R. Vrijen, *et al.*, *Phys. Rev. A* **62**, 012306 (2000)
G.P. Berman, G. D. Doolen, P. C. Hammel, and
V. I. Tsifrinovich, *Phys. Rev. B* **61**, 14694 (2000).

Advantages:

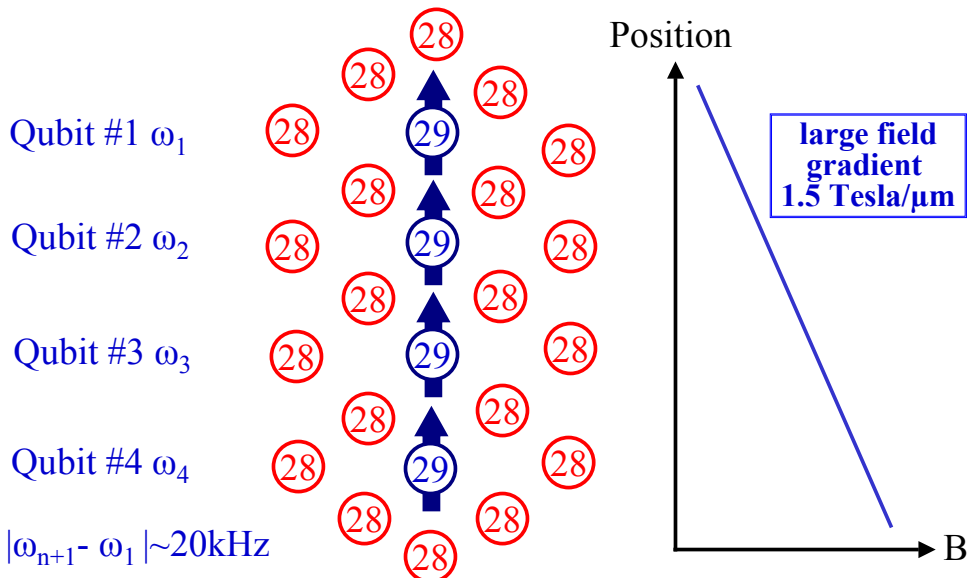
Scalable!
Can cool to low temperatures
for initialization

Disadvantages:

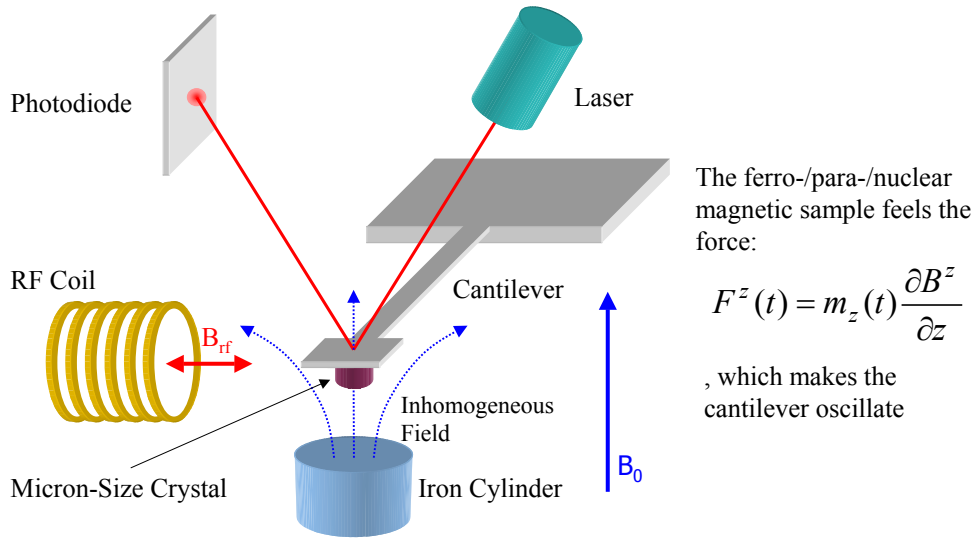
Need single-spin measurement
Challenging fabrication

All Silicon QC uses advantages of both!

^{29}Si nuclear spin quantum computer



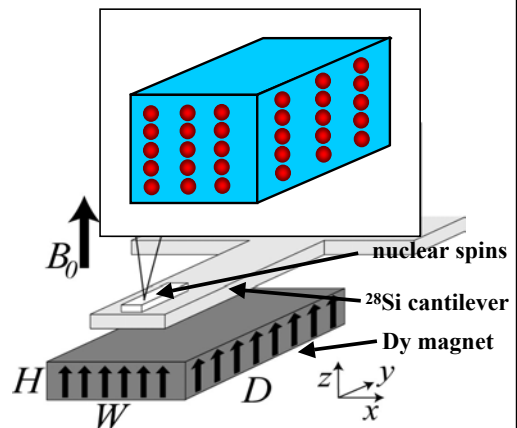
Magnetic Resonance Force Microscopy



An all silicon quantum computer

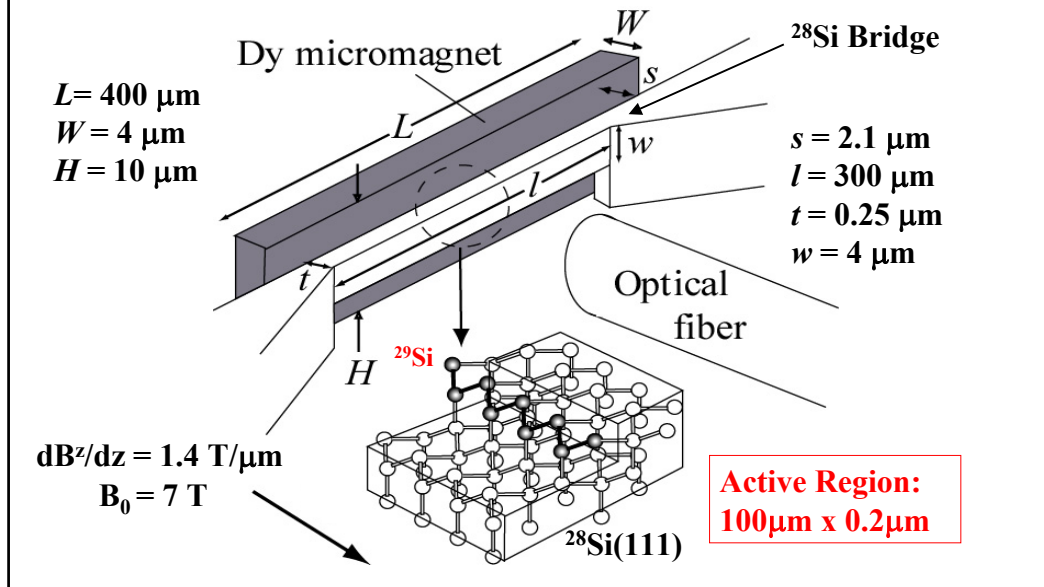
- **Qubits are spin-1/2 ^{29}Si nuclei in a ^{28}Si crystal.** They are distinguished by a one-dimensional **field gradient**.
- Initialization is accomplished by cooling, optical pumping, “boosting,” and “pseudo-pure state” techniques.
- Qubit interactions (**decoupling and recoupling**) are accomplished with RF pulse sequences.
- An ensemble of copies, orthogonal to the gradient direction, allow measurement by **MRFM**.
- Decoherence times are limited by pulse sequence design, crystal purity, and cantilever stability.

^{29}Si wires embedded in the ^{28}Si matrix



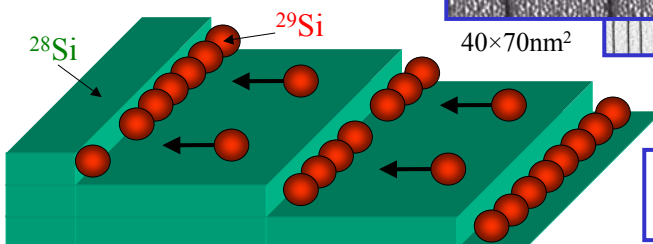
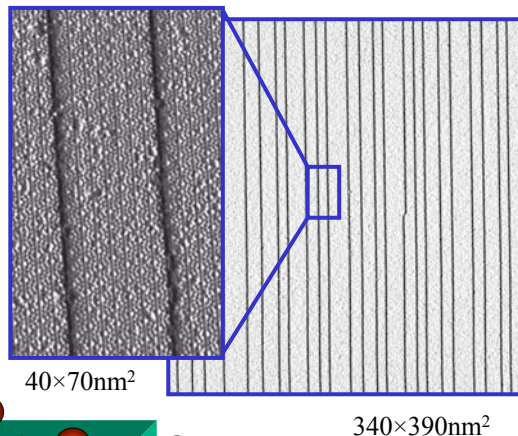
Improvement of Ladd, Goldman, Yamaguchi and Yamamoto, quant-ph/0009122 (2001)

Alternative configuration



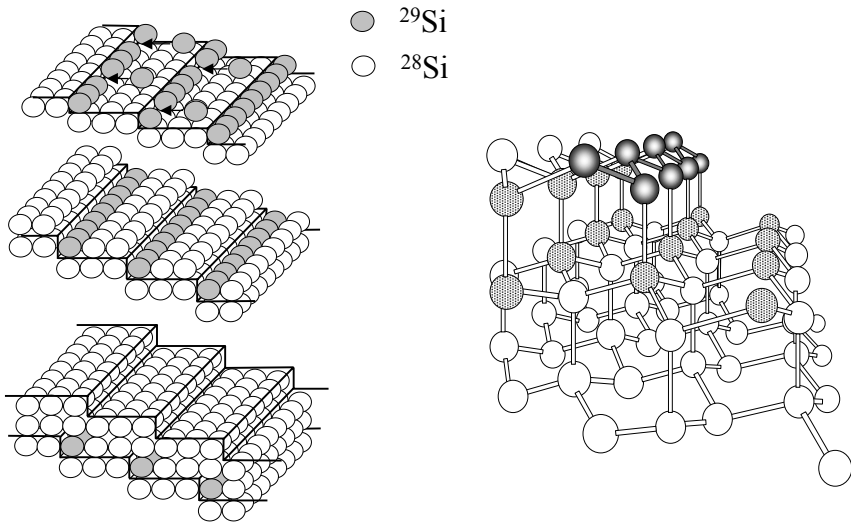
²⁹Si wire fabrication

- Form regular step arrays on slightly miscut ²⁸Si(111)7×7 surface ($\sim 1^\circ$ from normal)
- Steps are *straight*, with about 1 kink in 20000 sites.
- ²⁹Si chains formed by “Step Decoration” from ²⁸Si steps
- Angle of miscut controls chain spacing

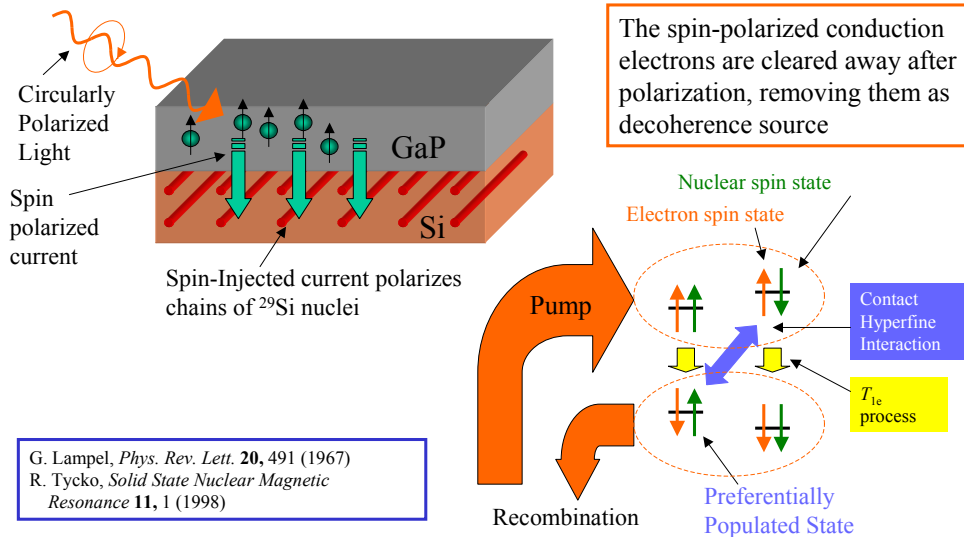


J.-L. Lin, *et al.*, *JAP*
84, 255 (1998)

MBE fabrication of ^{29}Si wire copies

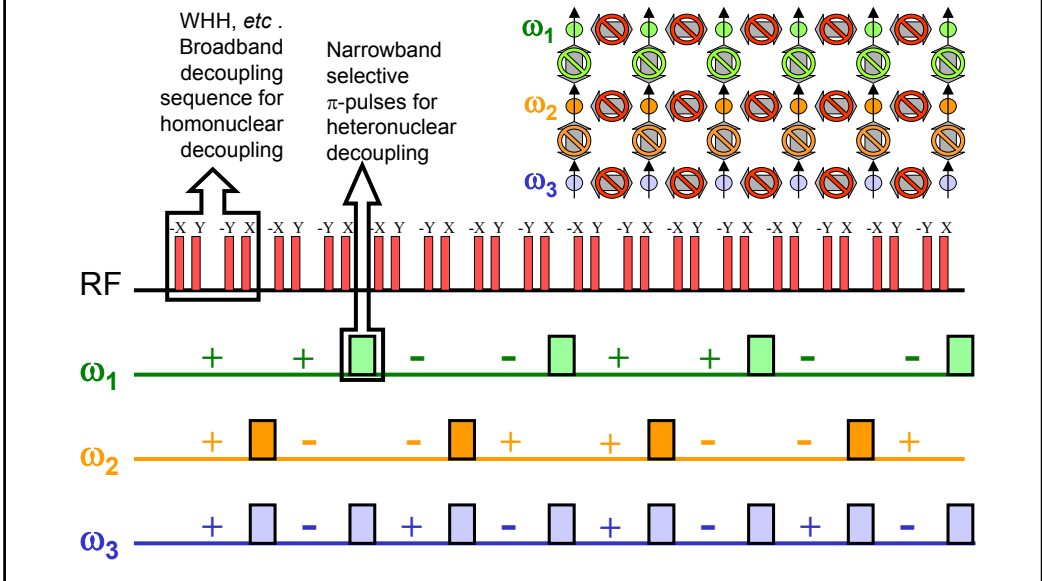


Polarization by optical pumping



G. Lampel, *Phys. Rev. Lett.* **20**, 491 (1967)
R. Tycko, *Solid State Nuclear Magnetic Resonance* **11**, 1 (1998)

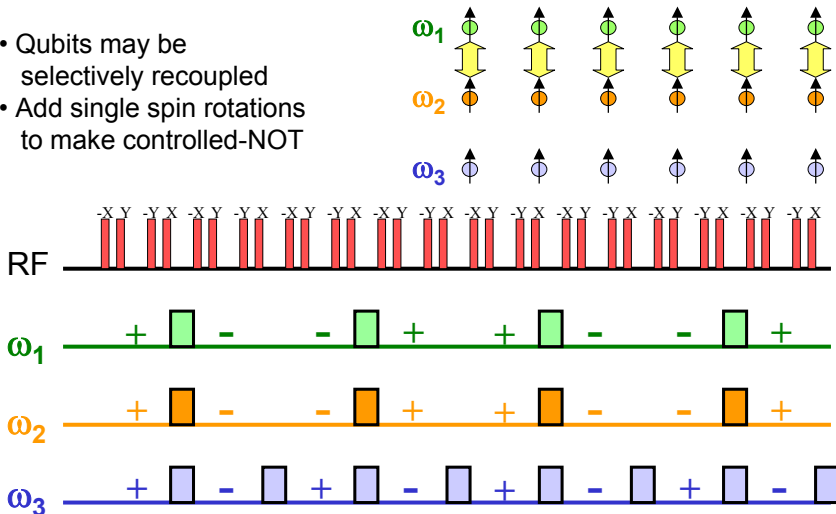
Operation (decoupling)



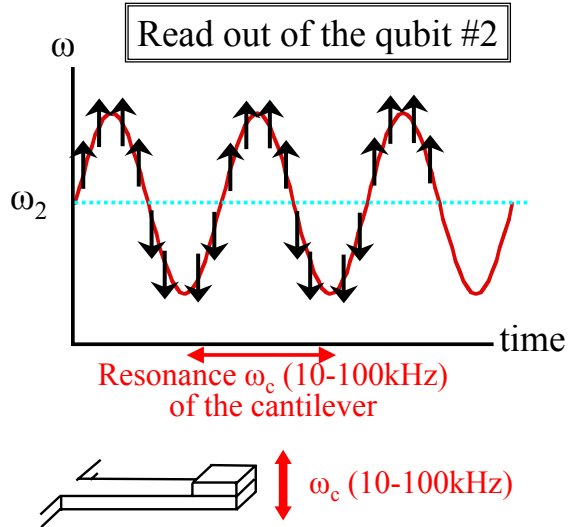
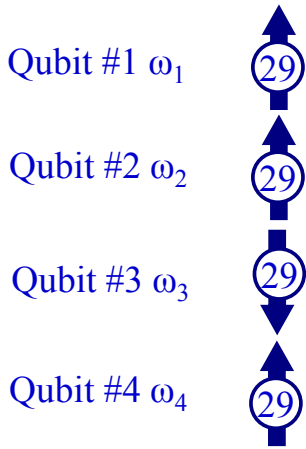
Operation (recoupling)

D. W. Leung, I. Chuang, F. Yamaguchi and Y. Yamamoto, Phys. Rev. A, 61(4) 042310/1 (1999)

- Qubits may be selectively recoupled
- Add single spin rotations to make controlled-NOT



Read-out by the MRFM cantilever



SNR and number of qubits

Force resolution for a cantilever in the thermal limit:

$$F_{\min} = \sqrt{4kk_B T B / \omega_0 Q}$$

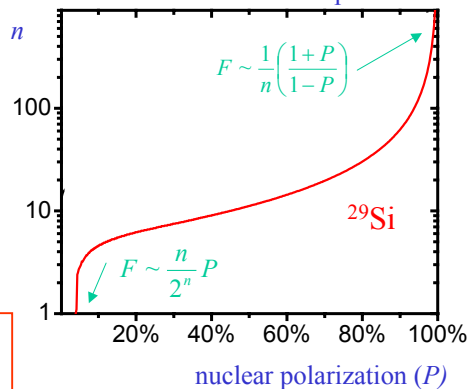
Force generated from a single atomic plane:

$$F(t) = M_z(r, t) \frac{\partial B_z}{\partial z}$$

Magnetization for nuclear spins in plane:

$$M_z = \gamma \hbar I N \left[\left(\frac{1+P}{2} \right)^n - \left(\frac{1-P}{2} \right)^n \right]$$

Number of qubits (n) for SNR = 1 vs. nuclear polarization



N = number of qubit copies
 n = number of qubits in QC

Decoherence and the maximum operation step

$$\frac{1}{T_2} = \frac{1}{2T_1} + \frac{\gamma^2}{2} \int_{-\infty}^{\infty} \langle \partial B_Z(t) \partial B_Z(0) \rangle dt + \left(\langle [H_{\text{dip}}^{\text{res}}, [H_{\text{dip}}^{\text{res}}, I^X]] \rangle / \langle I^X \rangle \right)^{1/2}$$

DC spectral density of local fluctuating field
Second Moment due to residual dipolar couplings

Primary Decoherence Sources:

Residual Dipolar Couplings

Reversible in principle
Present sequence: $T_2 \sim 10$ ms

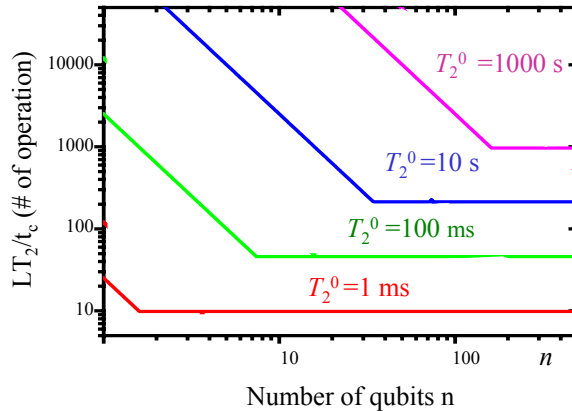
Cantilever Drift

Thermal equilibrium: $T_2 \sim 200$ ms
Feedback control $\Rightarrow T_2 \sim 1$ hour

Paramagnetic Impurities

Assuming very dilute impurities,
 $T_2 \sim (\omega_0 T_{1e})^{-1/2} T_1 \sim 1$ minute,
but much shorter for nuclei near impurity

Clock period $t_c = Ln^2 / \Delta\omega$ set by pulse sequence.
 \Rightarrow Number of logic gates T_2/t_c is limited

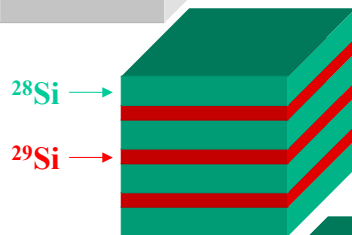


Step by step



Step.1 for Cantilever Fabrication & MRFM Readout

Few-hundred-nanometer-thick ^{29}Si on natural Si substrate



Step.2 toward Quantum Computation

$(^{29}\text{Si})_n / (^{28}\text{Si})_m$ isotope silicon superlattices with various n & m



Step.3 for First Logic Gates

Two single-layer of ^{29}Si as qubits

Our estimate allows a few logic gates in particular configurations, which are barely enough for “*proof of principle*”

Why ^{29}Si in ^{28}Si

- **Established crystal growth, processing and isotope engineering technologies**
- **Longest possible decoherence time**
No extrinsic electron and nuclear spins, reduced magnetic impurities
- **Minimum cross-talk between qubit copies but enough ensemble of qubit copies**
- **^{28}Si matrix provides natural means for optical pumping and detection of ^{29}Si nuclear spins**
- **Highest-possible-Q magnetic resonance force microscope (MRFM) cantilever**
- **Possible integration with Si CMOS and SET circuits**