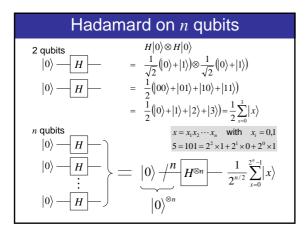
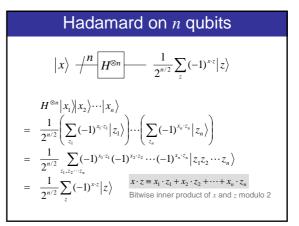
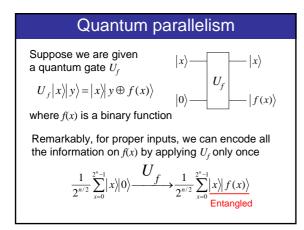
## Deutsch-Jozsa Algorithm

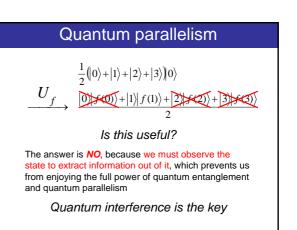
School on Quantum Computing @ Yagami Day 1, Lesson 3 13:00-14:00, March 22, 2005 Eisuke Abe Department of Applied Physics and Physico-Informatics, and CREST-JST, Keio University



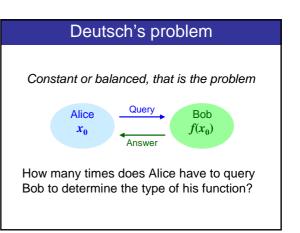


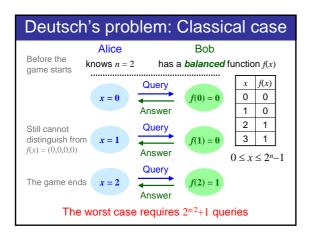


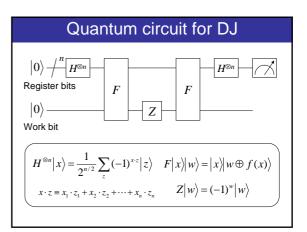


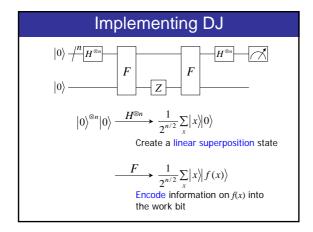


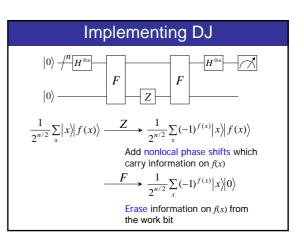
	Dei	utso	ch's	s pr	ob	len	n	
ary f	unctio			illed <b>c</b> lues c		<b>int</b> if	it ou	tputs
half		the po	ssibl	lled <b>b</b> e x, a nced	nd 1 f	or th		er half
x	f(x)		x	f(x)		x	f(x)	I
0	0		0	0		0	0	1
1	0		1	0		1	0	1
2	0		2	1		2	0	1
3	0		3	1		3	1	1
								-

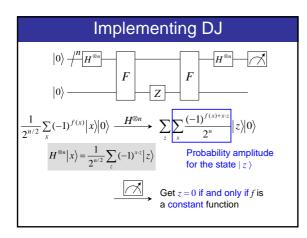


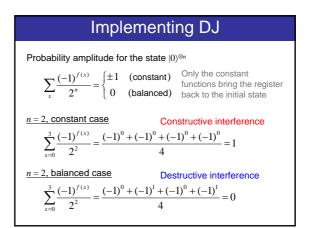


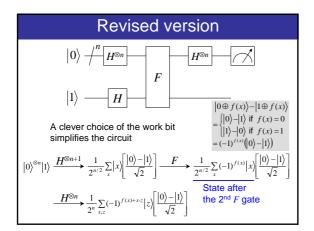


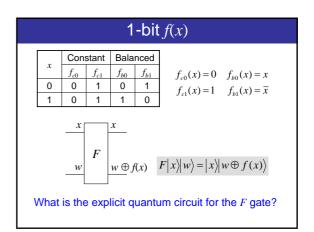


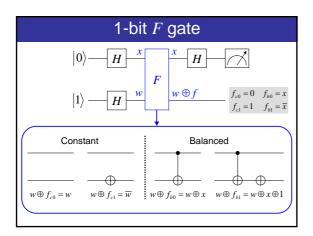


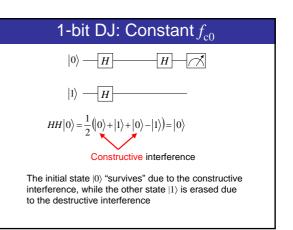


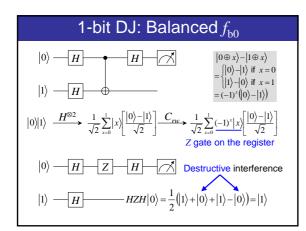




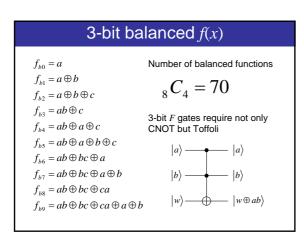




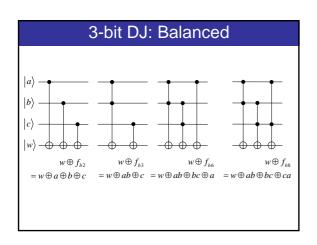


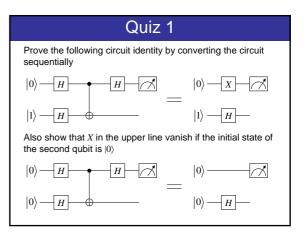


x	ab	Constant		Balanced ( $_4C_2 = 6$ )					
л	uv	$f_{c0}$	$f_{c1}$	$f_{b0}$	$f_{b1}$	$f_{b2}$	$f_{b3}$	$f_{b4}$	$f_{b5}$
0	00	0	1	0	0	0	1	1	1
1	01	0	1	0	1	1	1	0	0
2	10	0	1	1	0	1	0	1	0
3	11	0	1	1	1	0	0	0	1
	0.00		$\begin{array}{c} f_{b0} \\ f_{b1} \\ f_{b2} \end{array}$	(x) =	b	$f_{b4}($	$\begin{aligned} x) &= \overline{a} \\ x) &= \overline{b} \\ x) &= \overline{a} \end{aligned}$		



	3	3-k	oit	ba	lar	nce	ed	f(x	)		
x	abc	$f_{b0}$	$f_{b1}$	$f_{b2}$	$f_{b3}$	$f_{b4}$	$f_{b5}$	$f_{b6}$	$f_{b7}$	$f_{b8}$	$f_{b9}$
0	000	0	0	0	0	0	0	0	0	0	0
1	001	0	0	1	1	1	1	0	0	0	0
2	010	0	1	1	0	0	1	0	1	0	1
3	011	0	1	0	1	1	0	1	0	1	0
4	100	1	1	1	0	1	1	1	1	0	1
5	101	1	1	0	1	0	0	1	1	1	0
6	110	1	0	0	1	0	1	0	1	1	1
7	111	1	0	1	0	1	0	1	0	1	1
# o	f blcd fns	6	6	2	6	12	6	12	12	2	6
$f_{b0} = a$		$f_{\scriptscriptstyle b4} = ab \oplus a \oplus c \qquad \qquad f_{\scriptscriptstyle b8} = ab \oplus bc \oplus ca$									
$f_{b1} = a \oplus b$		$f_{\scriptscriptstyle b5} = ab \oplus a \oplus b \oplus c \qquad f_{\scriptscriptstyle b9} = ab \oplus bc \oplus ca \oplus a \oplus b$									
$f_{b2} = 0$	$a \oplus b \oplus c$	$f_{b6}$	= ab	$\oplus bc$	$\oplus a$						
$f_{b3} = 0$	$ab \oplus c$	$f_{\scriptscriptstyle b7}$	= ab	$\oplus bc$	$\oplus a \in$	₿b					





## Quiz 2

	ab	Constant		Balanced							
x	ар	$f_{c0}$	$f_{c1}$	$f_{b0}$	$f_{b1}$	$f_{b2}$	$f_{b3}$	$f_{b4}$	$f_{b5}$		
0	00	0	1	0	0	0	1	1	1		
1	01	0	1	0	1	1	1	0	0		
2	10	0	1	1	0	1	0	1	0		
3	11	0	1	1	1	0	0	0	1		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $											